

# CSCI427/927 Systems Development



## Alpha Algorithm in Process Mining **$\alpha$ -algorithm or $\alpha$ -miner**

# Definitions

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- Let  $T$  be a set of activities (Tasks) and  $T^*$  the set of all sequences of arbitrary length over  $T$ , then we have:
  - $\sigma \in T^*$  is called *execution sequence*, if all activities in  $\sigma$  belong to the same process instance
  - $W \subseteq T^*$  is called *execution log (workflow log)*
- Assumptions
  - In each process model, each activity appears at least once
  - Each direct neighbor relation between activities is represented at least once

# Execution Logs

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```
case 1 : task A
case 2 : task A
case 3 : task A
case 3 : task B
case 1 : task B
case 1 : task C
case 2 : task C
case 4 : task A
case 2 : task B
case 2 : task D
case 5 : task E
case 4 : task C
case 1 : task D
case 3 : task C
case 3 : task D
case 4 : task B
case 5 : task F
case 4 : task D
```

# Execution Logs

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Execution sequences:

Case 1: ABCD

Case 2: ACBD

Case 3: ABCD

Case 4: ACBD

Case 5: EF

Resulting

workflow log:

$W = \{ABCD, ACBD, EF\}$

```
case 1 : task A
case 2 : task A
case 3 : task A
case 3 : task B
case 1 : task B
case 1 : task C
case 2 : task C
case 4 : task A
case 2 : task B
case 2 : task D
case 5 : task E
case 4 : task C
case 1 : task D
case 3 : task C
case 3 : task D
case 4 : task B
case 5 : task F
case 4 : task D
```

# Order relations

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Log based order relations for pairs of activities  $a, b \in T$  in a workflow log  $W$ :

- Direct successor

$a \succ_w b$  i.e. in an execution sequence  $b$  directly follows  $a$

- Causality

$a \rightarrow_w b$  i.e.  $a \succ_w b$  and not  $b \succ_w a$

- Concurrency

$a \parallel_w b$  i.e.  $a \succ_w b$  and  $b \succ_w a$

- Exclusiveness

$a \#_w b$  i.e. not  $a \succ_w b$  and not  $b \succ_w a$

- *Activity pairs which never succeed each other*

# Execution log analysis

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□  $W = \{ABCD, ACBD, EF\}$

- Direct successor
- Causality
- Concurrency

```
case 1 : task A
case 2 : task A
case 3 : task A
case 3 : task B
case 1 : task B
case 1 : task C
case 2 : task C
case 4 : task A
case 2 : task B
case 2 : task D
case 5 : task E
case 4 : task C
case 1 : task D
case 3 : task C
case 3 : task D
case 4 : task B
case 5 : task F
case 4 : task D
```

# Execution log analysis

- $W = \{ABCD, ACBD, EF\}$ 
  - Direct successor
  - Causality
  - Concurrency

1)

A>B  
A>C  
B>C  
B>D  
C>B  
C>D  
E>F

2)

A→B  
A→C  
B→D  
C→D  
E→F

3)

B||C  
C||B

```
case 1 : task A
case 2 : task A
case 3 : task A
case 3 : task B
case 1 : task B
case 1 : task C
case 2 : task C
case 4 : task A
case 2 : task B
case 2 : task D
case 5 : task E
case 4 : task C
case 1 : task D
case 3 : task C
case 3 : task D
case 4 : task B
case 5 : task F
case 4 : task D
```

# $\alpha$ -Algorithm

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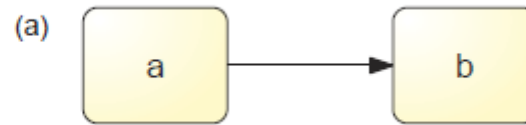
- The idea is to utilize order relations for deriving a **workflow net** that is compliant with these relations



# $\alpha$ -Algorithm

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## □ Idea (a)

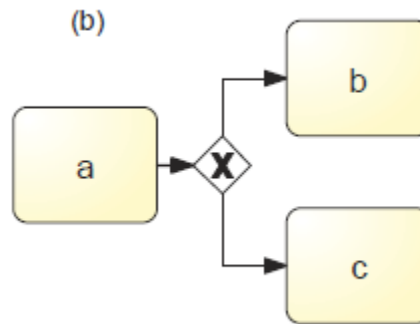


$$a \rightarrow b$$

# $\alpha$ -Algorithm

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## □ Idea (b)

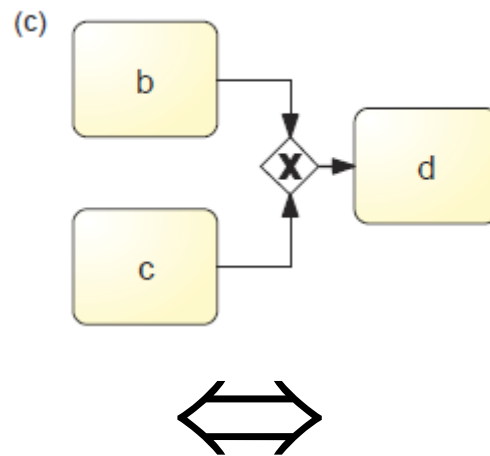


$a \rightarrow b, a \rightarrow c$  and  $b \# c$

# $\alpha$ -Algorithm

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## □ Idea (c)

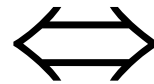
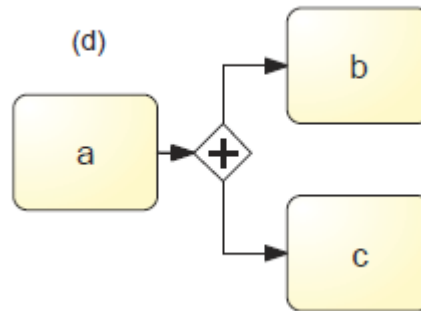


$b \rightarrow d, c \rightarrow d$  and  $b \# c$

# $\alpha$ -Algorithm

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## □ Idea (d)

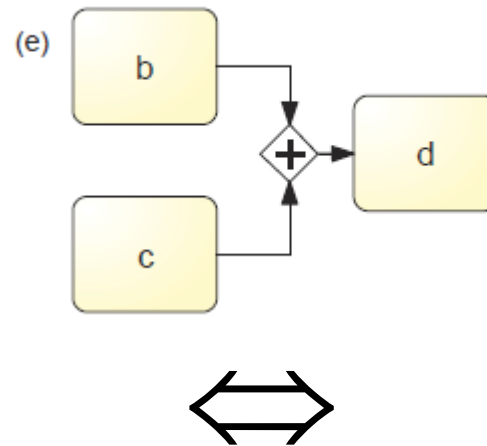


$a \rightarrow b, a \rightarrow c$  and  $b \parallel c$

# $\alpha$ -Algorithm

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## □ Idea (e)



$b \rightarrow d, c \rightarrow d$  and  $b \parallel c$

# The Alpha-Algorithm (simplified)

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1. Identify the set of **all tasks** in the log as  $T_W$ .
  2. Identify the set of all tasks that have been observed as the **first task** in some case as  $T_I$ .
  3. Identify the set of all tasks that have been observed as the **last task** in some case as  $T_O$ .
  4. Identify the set of all connections to be potentially represented in the process model as a set  $X_W$ . Add the following elements to  $X_W$ :
    - a. Pattern (a): all pairs for which hold  $a \rightarrow b$ .
    - b. Pattern (b): all triples for which hold  $a \rightarrow (b \# c)$ .
    - c. Pattern (c): all triples for which hold  $(b \# c) \rightarrow d$ .
- Note that triples for which Pattern (d)  $a \rightarrow (b || c)$  or Pattern (e)  $(b || c) \rightarrow d$  hold are not included in  $X_W$ .

# The Alpha-Algorithm (cont.)

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5. Construct the set  $Y_W$  as a subset of  $X_W$  by:
  - a. Eliminating  $a \rightarrow b$  and  $a \rightarrow c$  if there exists some  $a \rightarrow (b \# c)$ .
  - b. Eliminating  $b \rightarrow c$  and  $b \rightarrow d$  if there exists some  $(b \# c) \rightarrow d$ .
  
6. Connect start and end events in the following way:
  - a. If there are multiple tasks in the set  $T_I$  of first tasks, then draw a start event leading to an XOR-split, which connects to every task in  $T_I$ . Otherwise, directly connect the start event with the only first task.
  
  - b. For each task in the set  $T_O$  of last tasks, add an end event and draw an arc from the task to the end event.

# The Alpha-Algorithm (cont.)

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7. Construct the flow arcs in the following way:

- a. Pattern (a): For each  $a \rightarrow b$  in  $Y_W$ , draw an arc  $a$  to  $b$ .
- b. Pattern (b): For each  $a \rightarrow (b \# c)$  in  $Y_W$ , draw an arc from  $a$  to an XOR-split, and from there to  $b$  and  $c$ .
- c. Pattern (c): For each  $(b \# c) \rightarrow d$  in  $Y_W$ , draw an arc from  $b$  and  $c$  to an XOR-join, and from there to  $d$ .
- d. Pattern (d) and (e): If a task in the so constructed process model has multiple incoming or multiple outgoing arcs, bundle these arcs with an AND-split or AND-join, respectively.

8. Return the newly constructed process model.



# $\alpha$ -Algorithm Example

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case	1	:	task	A
case	2	:	task	A
case	3	:	task	A
case	3	:	task	B
case	1	:	task	B
case	1	:	task	C
case	2	:	task	C
case	4	:	task	A
case	2	:	task	B
case	2	:	task	D
case	5	:	task	E
case	4	:	task	C
case	1	:	task	D
case	3	:	task	C
case	3	:	task	D
case	4	:	task	B
case	5	:	task	F
case	4	:	task	D

# $\alpha$ -Algorithm Example

case	1	:	task	A
case	2	:	task	A
case	3	:	task	A
case	3	:	task	B
case	1	:	task	B
case	1	:	task	C
case	2	:	task	C
case	4	:	task	A
case	2	:	task	B
case	2	:	task	D
case	5	:	task	E
case	4	:	task	C
case	1	:	task	D
case	3	:	task	C
case	3	:	task	D
case	4	:	task	B
case	5	:	task	F
case	4	:	task	D

