

U

O

W

Guidelines Guidelines

# Functional Dependencies

CSIT882: Data Management Systems



UNIVERSITY  
OF WOLLONGONG  
AUSTRALIA

# Outline

- **Functional dependency ? What is it ?**
- Functional dependencies versus conceptual schemas
- Examples

# How good is your DB design?

## Information Preservation

- Does your design correctly capture all attributes, entities and relations?

## Minimum Redundancy

- Does your design minimize redundant storage of the same information and reduce the need for multiple updates?

# Example of Redundancy

Suppose we have a table *inst\_dept* which contain information for both *instructor* and *department*.

issue: possible repetition of information, which leads to **update anomalies**.

<i>ID</i>	<i>name</i>	<i>salary</i>	<i>dept_name</i>	<i>building</i>	<i>budget</i>
22222	Einstein	95000	Physics	Watson	70000
12121	Wu	90000	Finance	Painter	120000
32343	El Said	60000	History	Painter	50000
45565	Katz	75000	Comp. Sci.	Taylor	100000
98345	Kim	80000	Elec. Eng.	Taylor	85000
76766	Crick	72000	Biology	Watson	90000
10101	Srinivasan	65000	Comp. Sci.	Taylor	100000
58583	Califieri	62000	History	Painter	50000
83821	Brandt	92000	Comp. Sci.	Taylor	100000
15151	Mozart	40000	Music	Packard	80000
33456	Gold	87000	Physics	Watson	70000
76543	Singh	80000	Finance	Painter	120000

# Example of Redundancy

## Insertion Anomalies

- To insert a new employee, we must include the correct values for his/her department or NULLs.
- How to insert department with no employees?

## Deletion Anomalies

- What if we delete the last employee in a department?

## Update Anomalies

- What if we change the budget of a department?

<i>ID</i>	<i>name</i>	<i>salary</i>	<i>dept_name</i>	<i>building</i>	<i>budget</i>
22222	Einstein	95000	Physics	Watson	70000
12121	Wu	90000	Finance	Painter	120000
32343	El Said	60000	History	Painter	50000
45565	Katz	75000	Comp. Sci.	Taylor	100000
98345	Kim	80000	Elec. Eng.	Taylor	85000
76766	Crick	72000	Biology	Watson	90000
10101	Srinivasan	65000	Comp. Sci.	Taylor	100000
58583	Califieri	62000	History	Painter	50000
83821	Brandt	92000	Comp. Sci.	Taylor	100000
15151	Mozart	40000	Music	Packard	80000
33456	Gold	87000	Physics	Watson	70000
76543	Singh	80000	Finance	Painter	120000

# Devise a Theory for what is Good

We want to do two things:

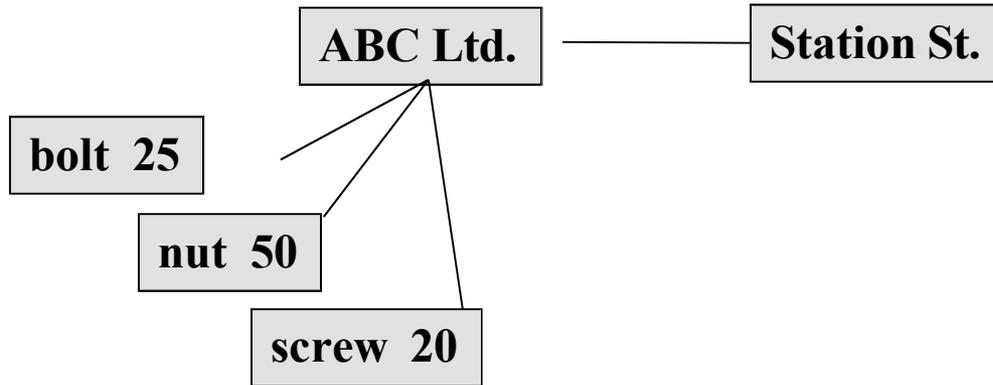
- Decide whether a particular relation  $R$  is in “good” form.
- If a relation  $R$  is not in “good” form, decompose it into a set of relations  $\{R_1, R_2, \dots, R_n\}$  such that
  - each relation is in good form
  - the decomposition is a lossless

Our theory/properties are defined based on **functional dependencies**.

# Functional dependency ? What is it ?

- Functional dependency describes the relationship between attributes.
    - It shows how attributes relate to other attributes.
  - Consider a relation schema  $R=(A, B)$ . If we know the value of A, we can only find at most one value of B in all the tuples of a relational table R. Then we have B functionally depends on A (or A functionally determines B)...
- ... We write  **$A \rightarrow B$**

# Functional dependency ? What is it ?



**Each warehouse is located at exactly one address**

**warehouse → warehouse-address**

**At each address there is only one warehouse**

**warehouse-address → warehouse**

**At each warehouse parts of the same kind have only one total quantity**

**warehouse, part → quantity**

# Functional dependency ? What is it ?

**Each car has one owner**

car → person

**Each child has one female parent**

child → female-parent

**Each child has one male parent**

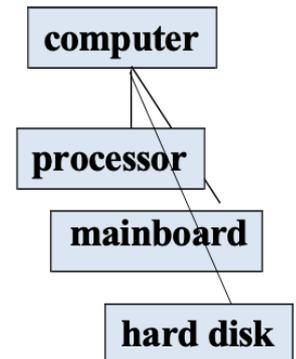
child → male-parent

**Each physical part belongs to one physical product**

physical-part → product

**Each physical product is sold by one retailer**

physical-product → retailer



# Outline

- Functional dependency ? What is it ?
- **Functional dependencies versus conceptual schemas**
- Examples

# How to identify functional dependencies

- Understand the meaning of each attribute.
- Find relationships between the attributes.
- Information may be found in the user's requirement specifications.
- Database designers use common sense to provide missing information.
- Use sample data – represent all possible data values that the database may hold.

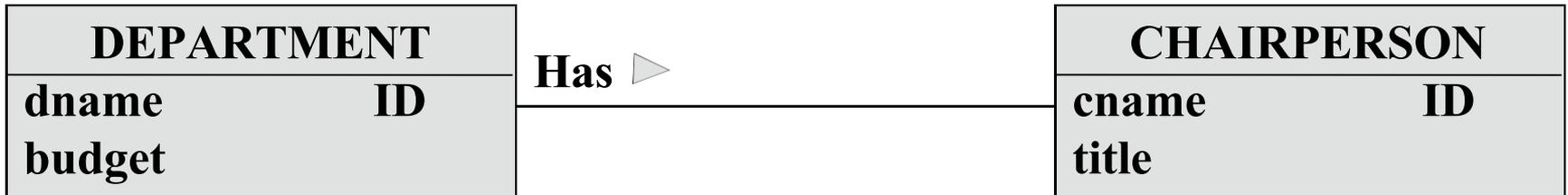
# Functional dependencies versus classes

STUDENT	
<b>s#</b>	<b>ID</b>
<b>name</b>	
<b>address</b>	
<b>language[1..*]</b>	

**s# → name**

**s# → address**

# Functional dependencies versus associations



**dname** → **budget**

**cname** → **title**

**dname** → **title**

**cname** → **budget**

**cname** → **dname**

**dname** → **cname**

# Functional dependencies versus associations



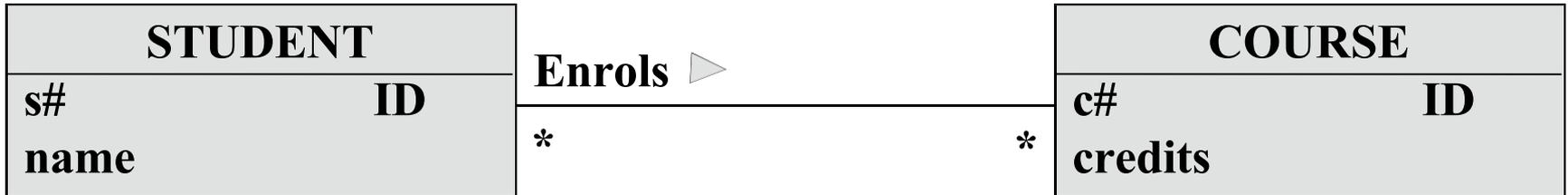
$emp\# \rightarrow name$

$p\# \rightarrow budget$

$emp\# \rightarrow p\#$

$emp\# \rightarrow budget$

# Functional dependencies versus associations



$s\# \rightarrow name$

$c\# \rightarrow credits$

# Outline

- Functional dependency ? What is it ?
- Functional dependencies versus conceptual schemas
- **Examples**

# Functional Dependencies

Consider a relation schema  $R=(A, B)$ . If we know the value of  $A$ , we can only find at most one value of  $B$  in all the tuples of a relational table  $R$ . ...  
...the functional dependency

$A \rightarrow B$  is true (holds)

ID	Name	Code	Grade
100	J	3550	A
200	X	3550	B
100	J	4540	B
100	J	4550	A

- Example:  $R = \{ID, Name, Code, Grade\}$ 
  - $ID \rightarrow Name$
  - $ID \rightarrow Grade,$                        $ID \rightarrow Code$
  - $ID, Name \rightarrow Grade,$                $ID, Code \rightarrow Grade$
  - $ID, Name \rightarrow Name$

Are they OK or not?

# Functional Dependencies

Consider a relation schema  $R=(A, B)$ . If we know the value of  $A$ , we can only find at most one value of  $B$  in all the tuples of a relational table  $R$ ...

...the functional dependency

$A \rightarrow B$  is true (holds)

ID	Name	Code	Grade
100	J	3550	A
200	X	3550	B
100	J	4540	B
100	J	4550	A

- Example:  $R = \{ID, Name, Code, Grade\}$ 
  - $ID \rightarrow Name$  (OK)
  - $ID \rightarrow Grade$  (not OK),       $ID \rightarrow Code$  (not OK)
  - $ID, Name \rightarrow Grade$  (not OK),       $ID, Code \rightarrow Grade$  (OK)
  - $ID, Name \rightarrow Name$  (trivial)

# Functional Dependencies: Test

Let's see if you understand (Test 1)

F:  $X \rightarrow Y$  (Assume FD  $X \rightarrow Y$ )

X Y

-----

a b

a ?

# Functional Dependencies: Test

Let's see if you understand (Test 2)

$F: X \rightarrow Y$

X Y

-----

a b

? b

c okay?

# Functional Dependencies: Test

Let's see if you understand (Test 3 & 4)

$$X, Y \rightarrow X$$

$$X \rightarrow X$$

**Note:** Functional dependencies like these are trivial

# Functional Dependencies: Test

Let's see if you understand (Test 5)

Consider R (A , B) with the following instances

1	4
1	5
3	7

$A \rightarrow B$  does NOT hold, but  $B \rightarrow A$  does hold.

## FD: relation between two sets

A functional dependency is a relation between two **sets** of attributes.

i.e., the value for a set of attributes determines the value for another set of attributes.

Examples:

$$XY \rightarrow WZ$$

$$XW \rightarrow Z$$

$$Z \rightarrow XQ$$

# Functional Dependencies

A WORKS\_ON relation

Ssn = social security number

Pnumber = project number

Question:

What might be the FDs of

WORKS\_ON?

WORKS\_ON

<u>Ssn</u>	<u>Pnumber</u>	Hours
123456789	1	32.5
123456789	2	7.5
666884444	3	40.0
453453453	1	20.0
453453453	2	20.0
333445555	2	10.0
333445555	3	10.0
333445555	10	10.0
333445555	20	10.0
999887777	30	30.0
999887777	10	10.0
987987987	10	35.0
987987987	30	5.0
987654321	30	20.0
987654321	20	15.0

## References

- Elmasri R., Navathe S. B., *Fundamentals of Database Systems*, chapter 10.2
- R. Ramakrishnan, J. Gehrke *Database Management Systems*, chapters 19.2, 19.3